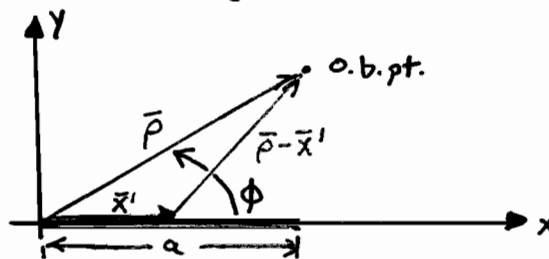


Once the TM^z and TE^z strip problems have been solved for the currents, we can calculate the total field everywhere in space.

Considering the TM^z scattering by a pec strip first \rightarrow

$$E_z^s(\bar{\rho}) = -jk\eta A_z(\bar{\rho}) = -\frac{k\eta}{4} \int_0^a J_z(x') H_0^{(2)}(k|\bar{\rho} - \bar{x}'|) dx' \quad (1)$$



For observation points far from the strip such that $k|\bar{\rho} - \bar{x}'| \rightarrow \infty$, the asymptotic form of the Hankel function

$$H_0^{(2)}(z) \sim \sqrt{\frac{jz}{\pi z}} e^{-jz}$$

with the approximations $|\bar{\rho} - \bar{x}'| \approx \begin{cases} \rho - x' \cos \phi & : \text{phase} \\ \rho & : \text{amplitude} \end{cases}$

gives

$$\begin{aligned} H_0^{(2)}(k|\bar{\rho} - \bar{x}'|) &\sim \sqrt{\frac{jz}{\pi k\rho}} e^{-jk(\rho - x' \cos \phi)} \\ &= \sqrt{\frac{jz}{\pi k\rho}} e^{-jk\rho} e^{jkx' \cos \phi} \end{aligned}$$

Substitution in (1)

$$E_z^s(\bar{\rho}) \sim -\frac{k\eta}{4} \sqrt{\frac{jz}{\pi k\rho}} e^{-jk\rho} \int_0^a J_z(x') e^{jkx' \cos \phi} dx' \quad (2)$$

Eqn. ② shows how the far field can be computed by a constant times the Fourier transform of the current. Since we used a pulse expansion for the current, the Fourier transform will be a sum of phase shifted sine functions. (No numerical integration is required.)

The above analysis can be repeated for all three Cartesian components and generalized to give the far-field

$$\vec{E}^s(\vec{p}) \sim -\frac{k\eta}{4} \sqrt{\frac{jz}{\pi k\rho}} e^{-jk\rho} \int_{S'} \vec{J}(\vec{p}') e^{j\vec{k}\cdot\vec{p}'} ds'$$

$$w) \quad \vec{k}\cdot\vec{p}' = k \cos\phi x' + k \sin\phi y'$$

which can be used for the TE^z scattering problem, for example.

In the far field, $E_\rho \rightarrow 0$ leaving E_z & E_ϕ non-vanishing components only, for the Z-D problem.

In a manner similar to 3-D problems, one can define a Radar Cross Section for Z-D geometries as an RCS per unit length. For Z-D problems this is referred to as an Echo Width or Z-D RCS, σ_{Z-D} . It is defined as -

The width intercepting the amount of incident power which, when radiated by cylindrical omni-directional radiation, produces at the receiver the same power density as the original target.

mathematically -
$$\lim_{\rho \rightarrow \infty} \left[\frac{\sigma_{2-D} P_i}{2\pi\rho} \right] = P_S$$

or

$$\underline{\underline{\sigma_{2-D} = \lim_{\rho \rightarrow \infty} \left[2\pi\rho \frac{P_S}{P_i} \right]}}$$

The definitions of monostatic and bistatic remain the same here for 2-D as for 3-D.

In decibels -

$$\sigma_{2-D} = 10 \log_{10} \left\{ \lim_{\rho \rightarrow \infty} 2\pi\rho \frac{P_S}{P_i} \right\}$$

in dbm or dB/λ.