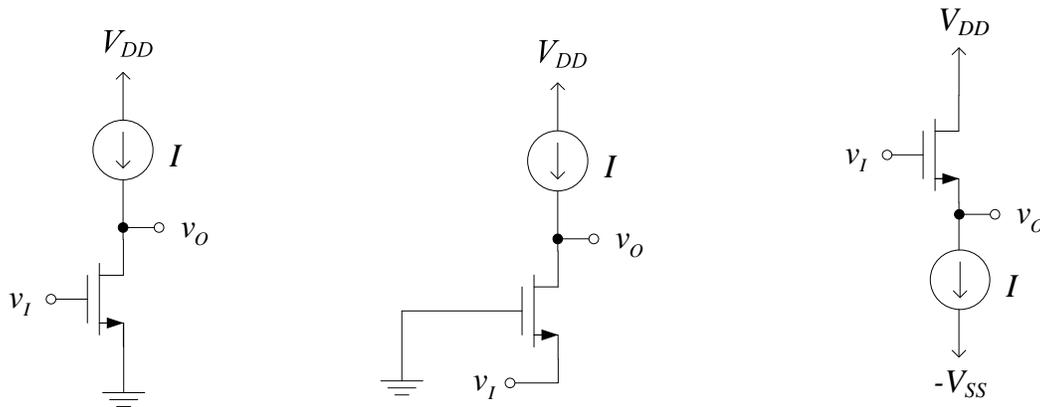


## Lecture 33: CMOS Common Source Amplifier.

As was mentioned in Lecture 30, there are two different environments in which MOSFET amplifiers are found, (1) discrete circuits and (2) integrated circuits (ICs). We will now begin to look at the **IC MOSFET amplifiers**.

There are **three basic configurations** of IC MOSFET amplifiers:



Common source

Common gate

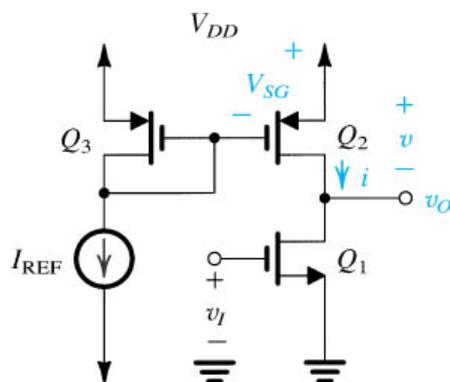
Common drain  
(source follower)

As was also mentioned in Lecture 30, large-valued resistors and capacitors are not often used in these IC environments. Instead, **active loads** are incorporated using MOSFETs as loads. In the amplifier circuits shown above, the **active loads are actually the nonideal current sources**. [Also notice that there are no bypass capacitors as we saw with discrete MOSFET (and BJT) amplifiers.]

We will look at all three of these amplifiers more closely over the next few lectures. The intention is to **pair the discrete version** of the MOSFET amplifier **with its IC version**. Since we've covered the CS amplifier in discrete form already, we'll begin with the analysis of the CMOS CS amplifier.

## CMOS Common Source Amplifier

An example of a complementary MOSFET amplifier is shown in text Figure 8.16(a), from Example 8.3:



(Fig. 8.16a)

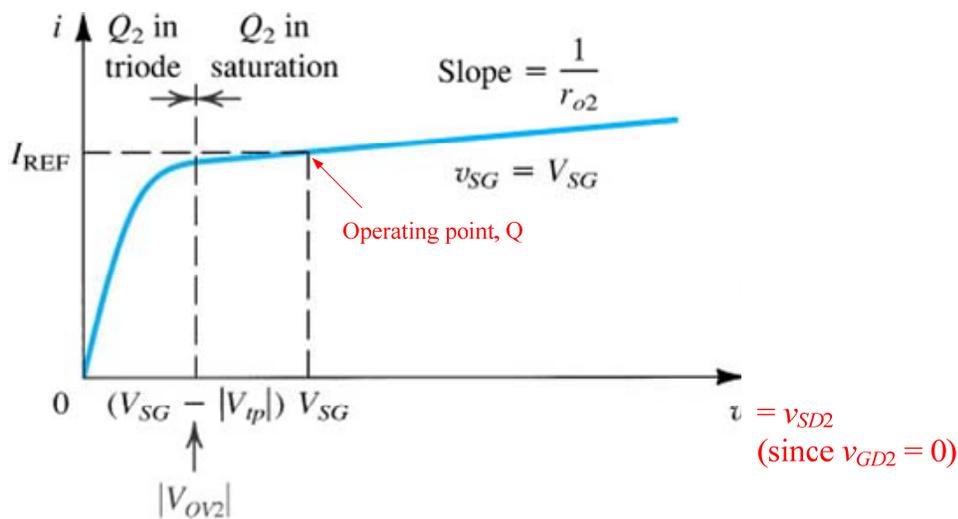
In this circuit,  $Q_2$  and  $Q_3$  form a PMOS current mirror. Because both PMOS and NMOS devices are used in this circuit, it is called a **complementary MOS (CMOS)** circuit.

In addition to forming part of the current mirror,  **$Q_2$  also functions as the current source load** (aka **active load**) for  $Q_1$ .

For  $Q_2$  to be a current source,  $Q_2$  must operate in the saturation mode, of course. The output resistance  $r_{o2}$  of  $Q_2$  is

$$r_{o2} = \frac{|V_{A2}|}{I_{REF}} \quad (8.48), (1)$$

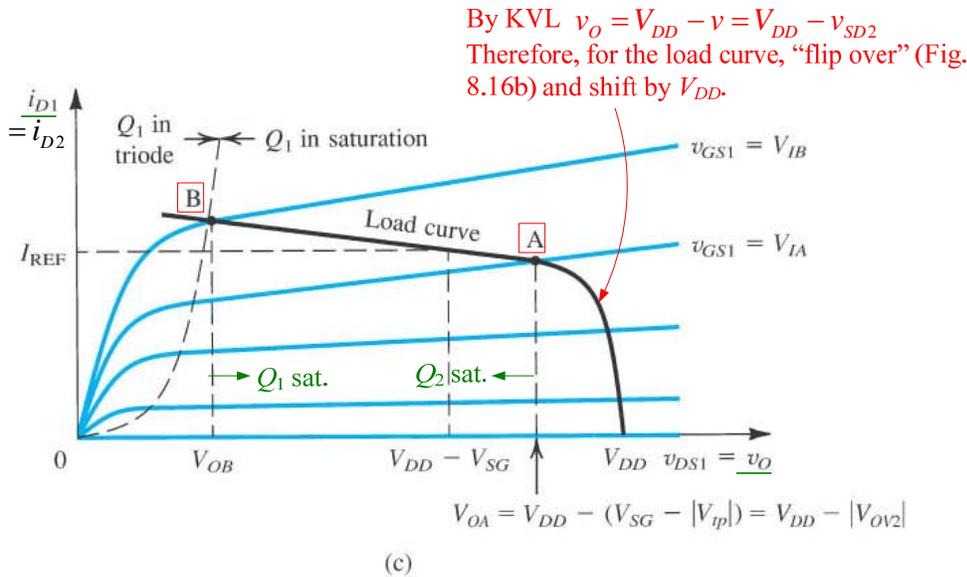
It is helpful to observe the characteristic curve for  $Q_2$  to understand its active-load role:



(Fig. 8.16b)

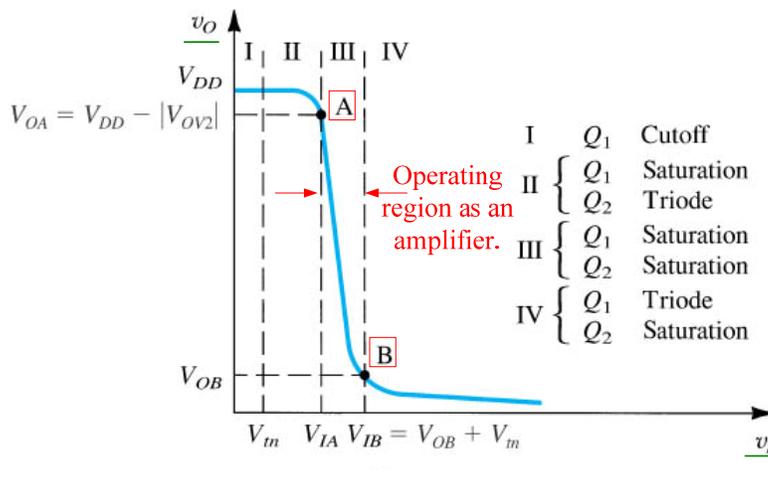
Referring to the CS amplifier circuit above in Fig. 8.16(a), when  $i = I_{REF}$  then  $V_{GD2} = 0$  (by **symmetry** with  $Q_1$ ). This implies that  $v = V_{SG}$ , which is the Q point shown in Fig. 8.16(b).

Furthermore, it is useful to observe the graphical construction of the transfer function  $v_o/v_I$  for this amplifier, as illustrated in Figs. 8.16(c) and (d) shown below. The drain currents of  $Q_1$  and  $Q_2$  are the same. The **operating point** of the amplifier is found from the intersection of the  $Q_1$  characteristic curve with the load curve of  $Q_2$  for a particular  $v_{GS1}$ :



(Fig. 8.16c)

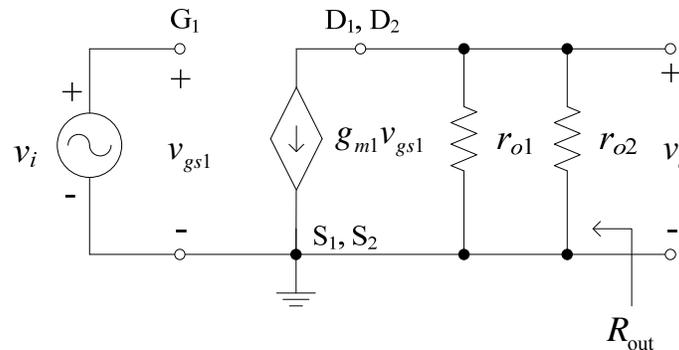
Collecting these intersections from this figure as  $v_{GS1}$  ( $= v_I$ ) changes, we can construct point-by-point the **transfer characteristic curve** for this amplifier:



From this plot, we can see that Region III shows a linear relationship between  $v_O$  and  $v_I$ . This is the region where the circuit of Fig. 8.16(a) can be used as a linear amplifier.

## Small-Signal Voltage Gain and Output Resistance

Now we'll determine the **small-signal voltage gain and output resistance** of this amplifier. The small-signal equivalent circuit for this CMOS CS amplifier is:



It is important to recognize that **no small-signal model is needed for  $Q_2$**  because its effect on the signal  $v_o$  can be incorporated using the **small-signal resistance  $r_{o2}$**  as shown above.

So, at the output

$$v_o = -g_{m1}v_{gs1}(r_{o1} \parallel r_{o2}) \quad (2)$$

while at the input

$$v_{gs1} = v_i \quad (3)$$

Substituting (3) into (2) gives the **open circuit small-signal voltage gain** for the CMOS CS amplifier to be

$$A_{vo} \equiv \frac{v_o}{v_i} = -g_{m1}(r_{o1} \parallel r_{o2}) \quad (8.49), (4)$$

Substituting into this expression for  $g_{m1}$

$$g_{m1} = \sqrt{2k_n'(W/L)_1 \sqrt{I_{D1}}} \quad (7.41)$$

and for  $r_{o1}$  and  $r_{o2}$  using

$$r_o = \frac{|V_A|}{I_D} \quad (7.37)$$

while noting that  $I_{D1} = I_{D2}$ , and then simplifying gives

$$A_{vo} = -\frac{\sqrt{2k_n' \left(\frac{W}{L}\right)_1} \frac{1}{\sqrt{I_{REF}}}}{\frac{1}{|V_{A1}|} + \frac{1}{|V_{A2}|}} \quad (5)$$

Since  $r_{o1}$  and  $r_{o2}$  are usually large, this  $A_{vo}$  gain is typically relatively large (approximately -20 to -100, or so).

Neat! We have incorporated the effects of relatively large resistance for this amplifier **without having to actually construct a large resistor**.

From the small-signal model we see from inspection that

$$R_{out} = r_{o1} \parallel r_{o2}$$

Summary for CMOS CS amplifier:

1. Very large input resistance.
2. Very large output resistance.
3. Potentially large small-signal voltage gain.

**Example N33.1** (similar to text Example 8.4). A CMOS CS amplifier shown in Fig. 8.16(a) is fabricated with

$W/L = 100 \mu\text{m}/1.6 \mu\text{m}$  for all transistors. With  $k_n' = 90 \mu\text{A}/\text{V}^2$ ,  $k_p' = 30 \mu\text{A}/\text{V}^2$ ,  $I_{\text{REF}} = 100 \mu\text{A}$ ,  $V_{A_n} = 8 \text{ V}/\mu\text{m}$ , and  $V_{A_p} = 12 \text{ V}/\mu\text{m}$ , determine the following quantities:

(a) Find  $g_{m1}$ . The common expression for  $g_m$  we use is

$$g_m = k_n' \frac{W}{L} (V_{GS} - V_t) \quad (7.40), (6)$$

For a MOSFET in the saturation mode

$$I_D = \frac{1}{2} k_n' \frac{W}{L} (V_{GS} - V_t)^2 \quad (7)$$

Substituting (7) into (6) gives the transconductance for  $Q_1$  in terms of  $I_{D1}$  to be

$$g_{m1} = \sqrt{2k_n' \left(\frac{W}{L}\right)_1 I_{D1}} \quad (7.41), (8)$$

[This form of  $g_m$  was actually used earlier in (5).] Because the amplifier is biased so that  $I_{D1} = I_{\text{REF}}$ , then

$$g_{m1} = \sqrt{2 \cdot 90 \times 10^{-6} \cdot \frac{100}{1.6} \cdot 100 \times 10^{-6}} = \mathbf{1.06 \text{ mA/V}}$$

(b) Find  $r_{o1}$ . Notice the units for  $V_{A_n}$  and  $V_{A_p}$  are  $\text{V}/\mu\text{m}$ . This output resistance is proportional to the channel length  $L$ .

$$r_{o1} = \frac{|V_A|_1}{I_{D1}} = \frac{V_{A_n} \cdot L}{I_{\text{REF}}} = \frac{8 \cdot 1.6}{100 \times 10^{-6}} = \mathbf{128 \text{ k}\Omega}$$

(c) Find  $r_{o2}$ .

$$r_{o2} = \frac{|V_A|_2}{I_{D2}} = \frac{V_{Ap} \cdot L}{I_{REF}} = \frac{12 \cdot 1.6}{100 \times 10^{-6}} = 192 \text{ k}\Omega$$

(d) Find  $A_{vo}$ .

$$A_{vo} = -g_m (r_{o1} \parallel r_{o2}) = -1.06 \times 10^{-3} (128 \text{ k}\Omega \parallel 192 \text{ k}\Omega)$$

$$A_{vo} = -81.4 \frac{\text{V}}{\text{V}}$$

This value represents the largest gain. The gain will be reduced when actual source and load impedances are attached to the amplifier.